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a) $(x,y) \in R$ iff $x+y$

- not reflexive because $(x,x) \notin R$

- symmetric, because $(x,y) \in R$ and $(y,x) \in R$
because $x+y$

- not antisymmetric, because $(x,y) \in R$ and $(y,x) \in R$
but $x \neq y$

- not transitive, because given (x,y) and (y,x) we
don't have (x,x)

e) $(x,y) \in R$ iff x is a multiple of y

- reflexive because x is a multiple of x , i.e. $(x,x) \in R$

- not symmetric, because 4 is a multiple of 2, but
not vice versa

- not antisymmetric, because if $(x,y) \in R$ then $(y,x) \notin R$
(see explanation for "not symmetric" above)

exception: 3 is a multiple of -3, but -3 is a multiple of 3

- transitive, because if $(x,y) \in R$ and $(y,z) \in R$ then

it means that $x = ky$, $k \in \mathbb{Z}$, and $y = mz$, $m \in \mathbb{Z}$,
so $x = kmz$, i.e. $(x,z) \in R$.

with numbers: if 8 is a multiple of 4, and
4 is a multiple of 2, then 8 is a multiple of 2.

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f) $(x,y) \in R$ iff x and y are both negative or both non-negative.

- reflexive, because $(x,x) \in R$
- symmetric, because if $(x,y) \in R$, then $(y,x) \in R$
(signs do not change)
- not antisymmetric, because if $(x,y) \in R$ and $(y,x) \in R$
it does not guarantee that $x = y$
example: $(2,3) \in R$ and $(3,2) \in R$, but $2 \neq 3$
- transitive, because if $(x,y) \in R$ and $(y,z) \in R$ it
means that x, y and z have the same sign,
i.e. $(x,z) \in R$ as well.